



Observatoire
de la CÔTE d'AZUR



INSU
Observer & comprendre



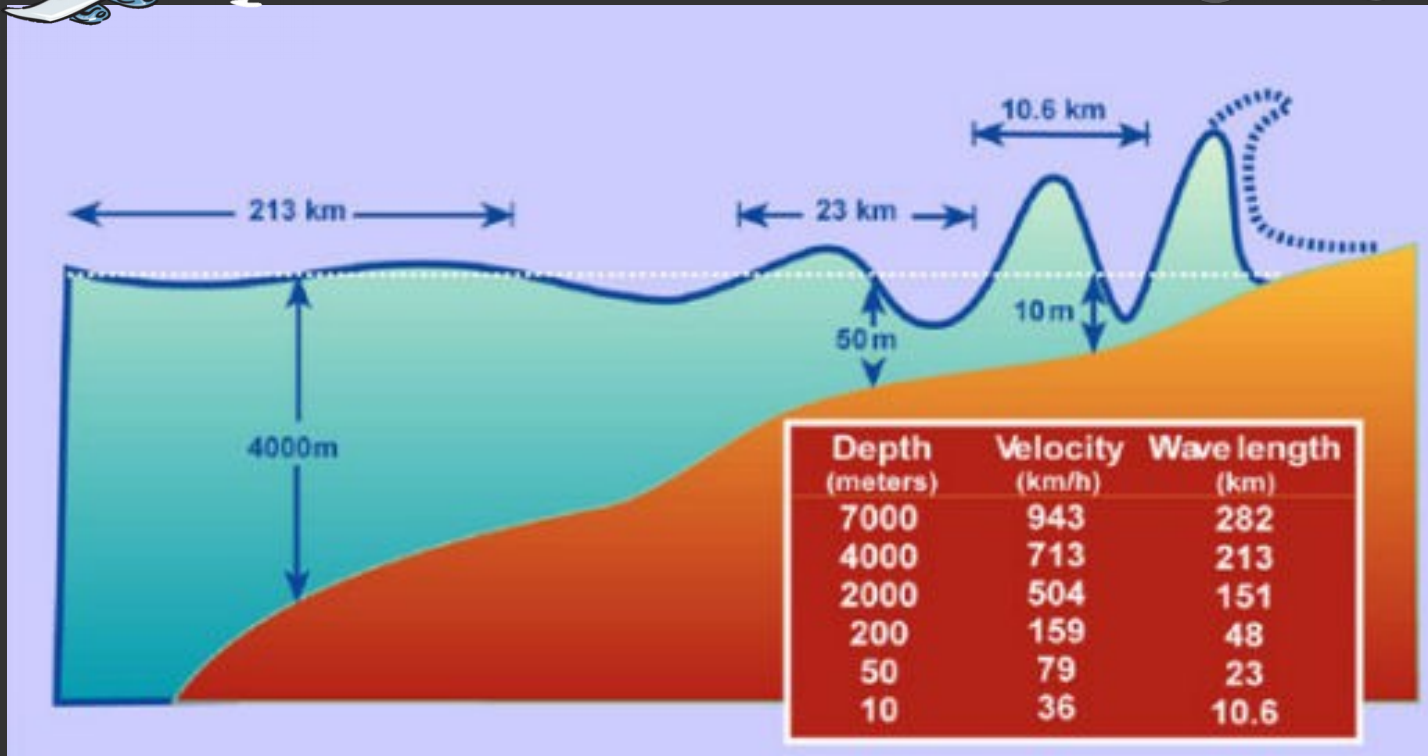
Inversion of tsunami data



A. Sladen – CNRS, Géoazur

DEFINITION

Tsunami waves are gravity wave with a long period
→ need a BIG source !



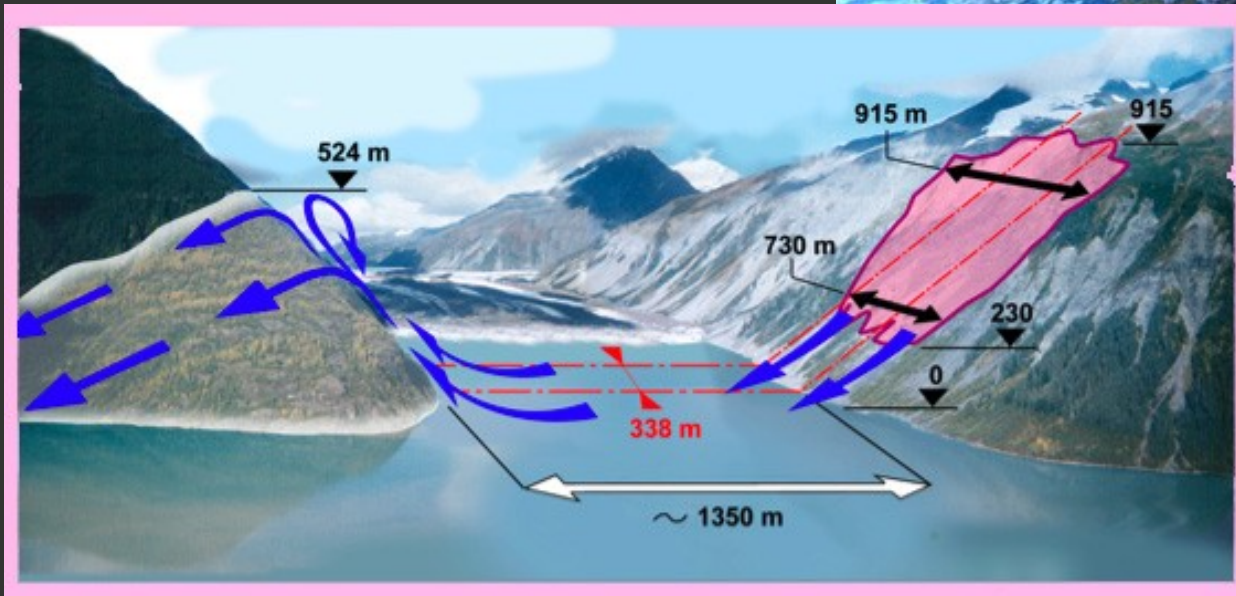
DEFINITION



Krakatoa, 1883

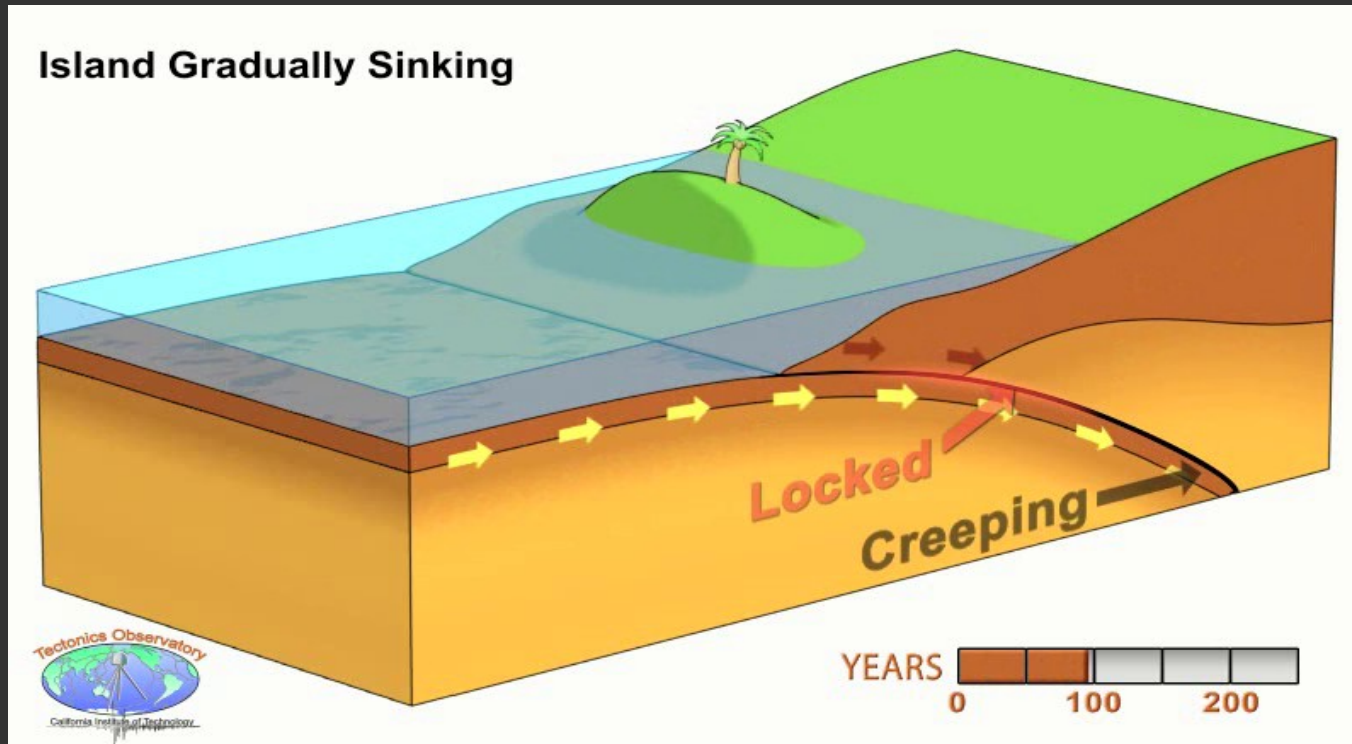


*Summer 2015,
E.T. pers. comm.*

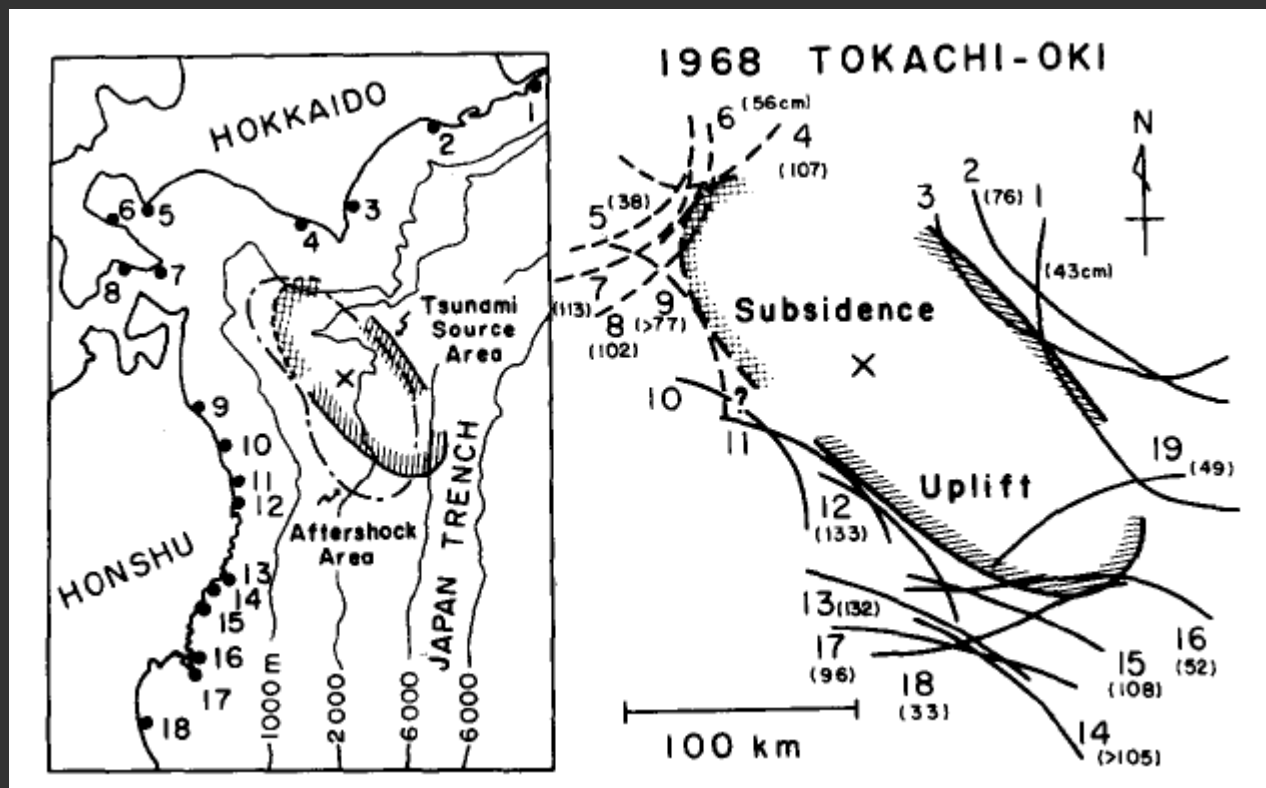


Lituya Bay, Alaska, 1958

DEFINITION



M_w 8.3 Tokachi-Oki 1968

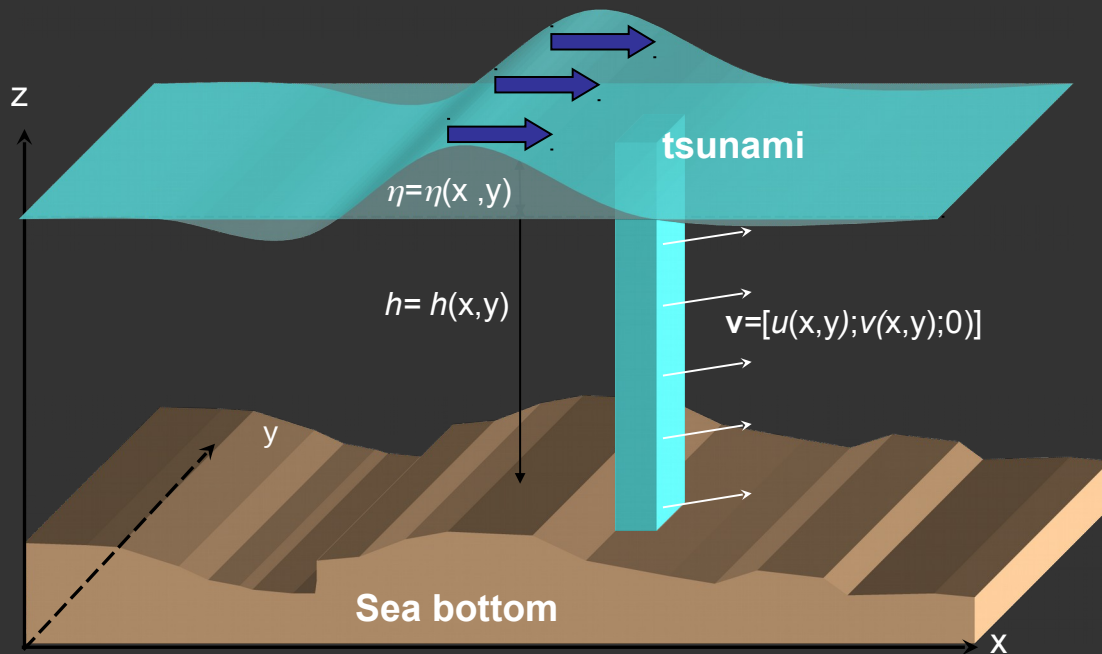


K.Abe, 1973

Tsunami equations

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- Assume full-instantaneous transfer of deformation to water column (incompressible)
- Shallow-water equations: depth-average Navier-stokes for long wavelengths (vs depth), only force is gravity, no viscous effect
- linear long wave ($\lambda \gg h$) leads to : $c = \sqrt{gh}$



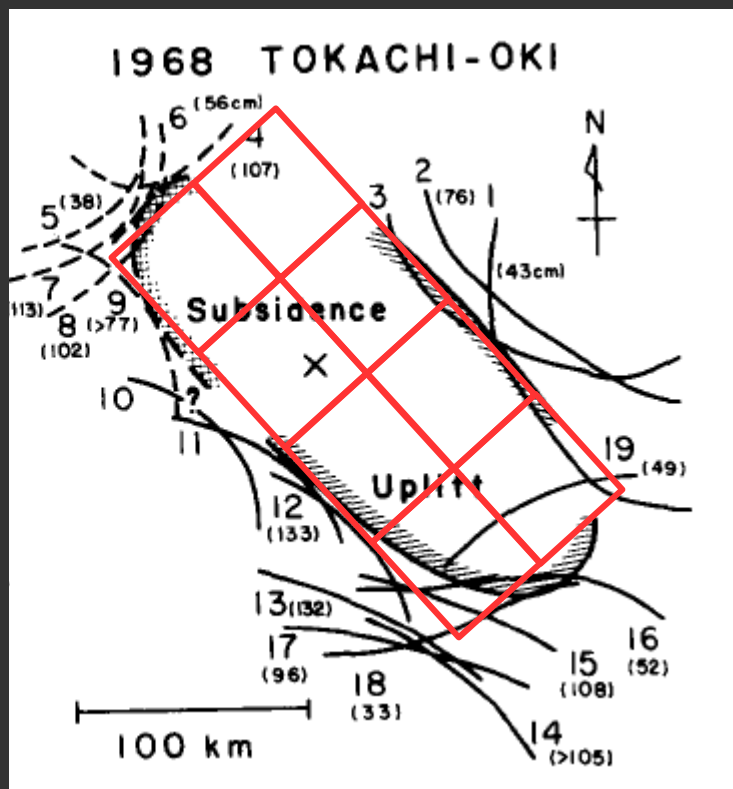
$$\frac{\partial(\eta + h)}{\partial t} + \nabla \cdot [\mathbf{v}(\eta + h)] = 0$$

$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\mathbf{g} \cdot \nabla \eta + \Sigma \mathbf{f}$$

g gravity
v horizontal velocity
η sea surface height

Tokachi-Oki 1968

Inversion for seafloor deformation

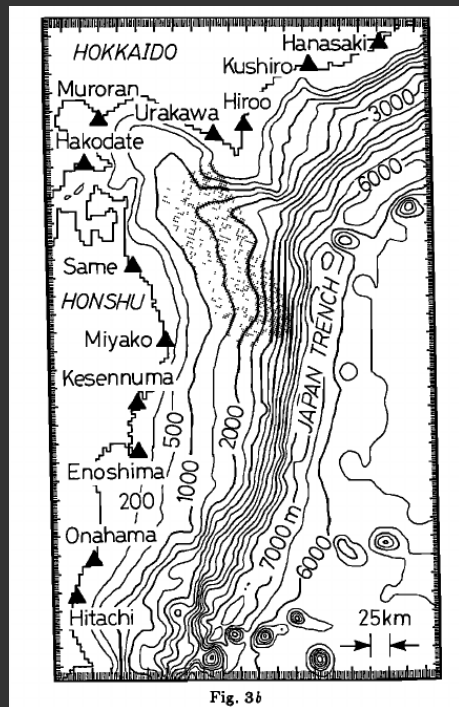


$$\begin{array}{c}
 \text{computed} \\
 \text{wavelorm at station 1} \\
 \left[\begin{array}{ccc}
 A_{11}(t_1) & A_{12}(t_1) & \dots & A_{1m}(t_1) \\
 A_{11}(t_2) & A_{12}(t_2) & \dots & A_{1m}(t_2) \\
 \vdots & \vdots & & \vdots
 \end{array} \right] \\
 \text{computed} \\
 \text{wavelorm at station 2} \\
 \left[\begin{array}{ccc}
 A_{21}(t_1) & A_{22}(t_1) & \dots & A_{2m}(t_1) \\
 A_{21}(t_2) & A_{22}(t_2) & \dots & A_{2m}(t_2) \\
 \vdots & \vdots & & \vdots
 \end{array} \right] \\
 \vdots \\
 \text{computed} \\
 \text{wavelorm at station k} \\
 \left[\begin{array}{ccc}
 A_{k1}(t_1) & A_{k2}(t_1) & \dots & A_{km}(t_1) \\
 A_{k1}(t_2) & A_{k1}(t_2) & \dots & A_{km}(t_2) \\
 \vdots & \vdots & & \vdots
 \end{array} \right]
 \end{array}
 \cdot
 \begin{array}{c}
 \left[\begin{array}{c}
 X_1 \\
 X_2 \\
 \vdots \\
 \vdots \\
 X_m
 \end{array} \right]
 \end{array}
 \approx
 \begin{array}{c}
 \text{segment 1} \\
 \left[\begin{array}{c}
 b_1(t_1) \\
 b_1(t_2) \\
 \vdots
 \end{array} \right] \\
 \text{segment 2} \\
 \left[\begin{array}{c}
 b_2(t_1) \\
 b_2(t_2) \\
 \vdots
 \end{array} \right] \\
 \vdots \\
 \text{segment m} \\
 \left[\begin{array}{c}
 b_m(t_1) \\
 b_m(t_2) \\
 \vdots
 \end{array} \right]
 \end{array}$$

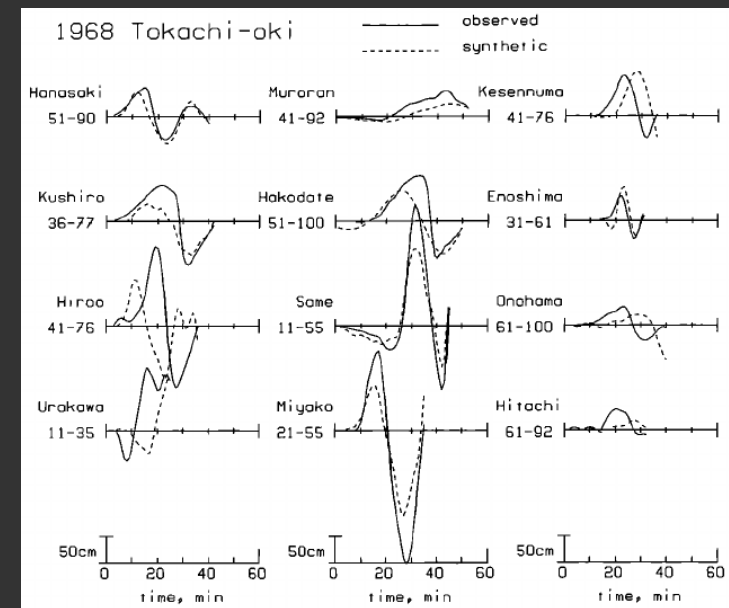
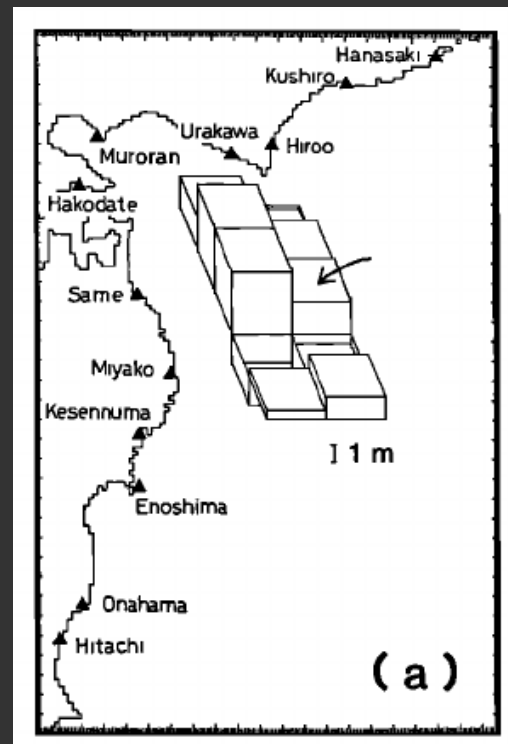
Fig. 4. Matrix representation of Eq. (4).

$$A_{ij}(t) \cdot x_j = b_i(t) \quad (4)$$

Tokachi-Oki 1968



bathymetric grid
resolution ~2.5km



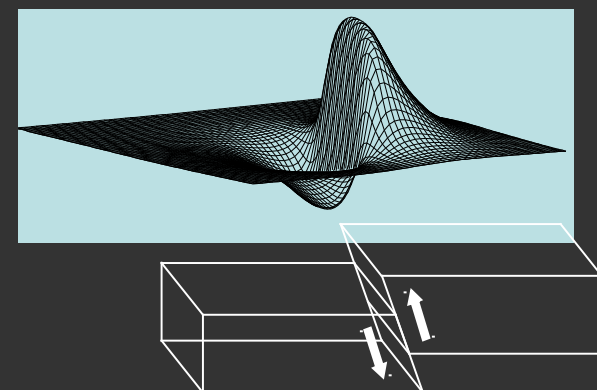
One big limitation

Inversion of tide gauge records ~linear only if large event and inverting 1st oscillation. Tide gauge should not be hidden deep inside a harbor maze

Tsunami data inversion

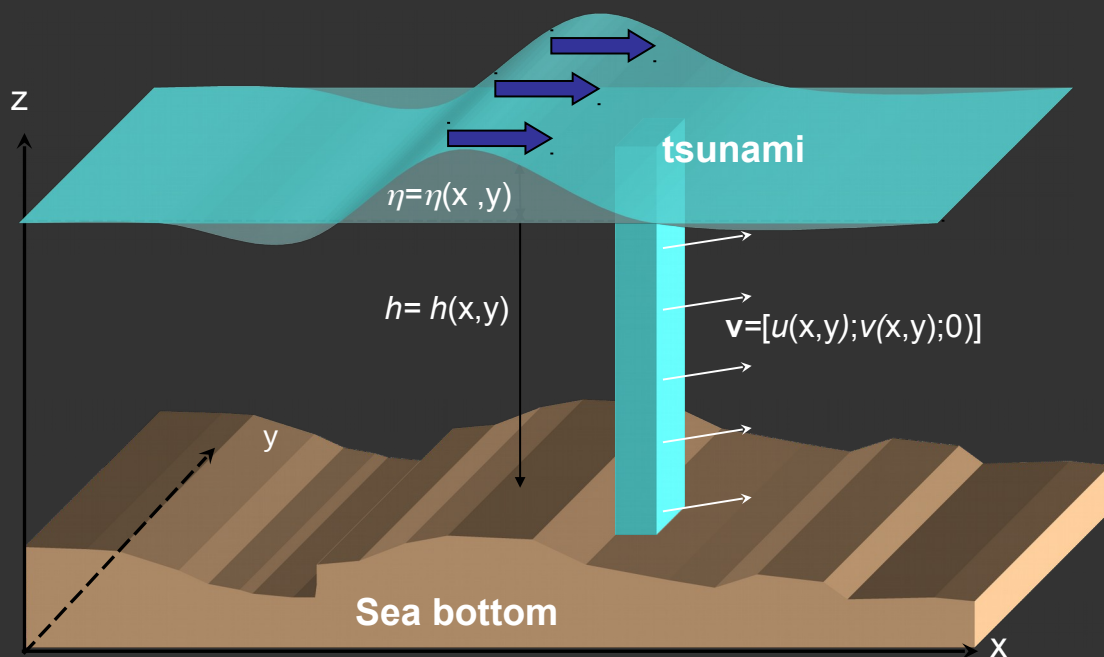
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- Sea-floor deformation caused by earthquake elastic dislocation (e.g. with Okada[1985])
- Assume full-instantaneous transfer of deformation to water column (incompressible)
- Shallow-water equations: depth-average Navier-stokes for long wavelengths
- linear long wave ($\lambda \gg h$) leads to : $c = \sqrt{gh}$



$$M_0 = \mu ULW$$

M_0 seismic moment
 U displacement
 μ rigidity
 L (W) fault length (width)

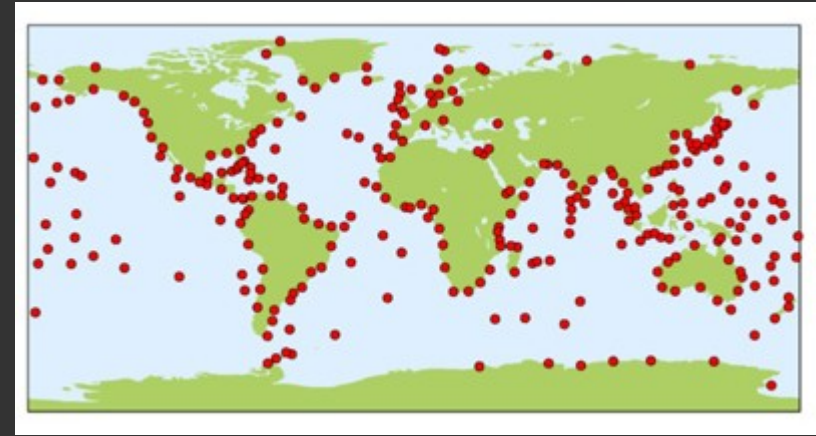


$$\frac{\partial(\eta + h)}{\partial t} + \nabla \cdot [\mathbf{v}(\eta + h)] = 0$$

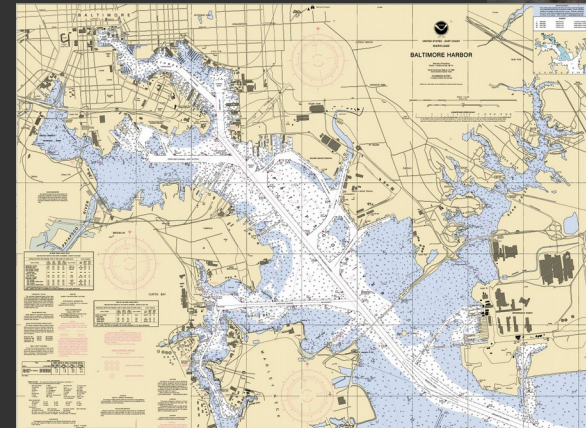
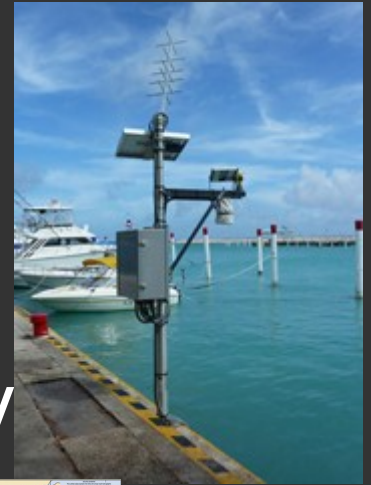
$$\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\mathbf{g} \cdot \nabla \eta + \Sigma \mathbf{f}$$

g gravity
v horizontal velocity
η sea surface height

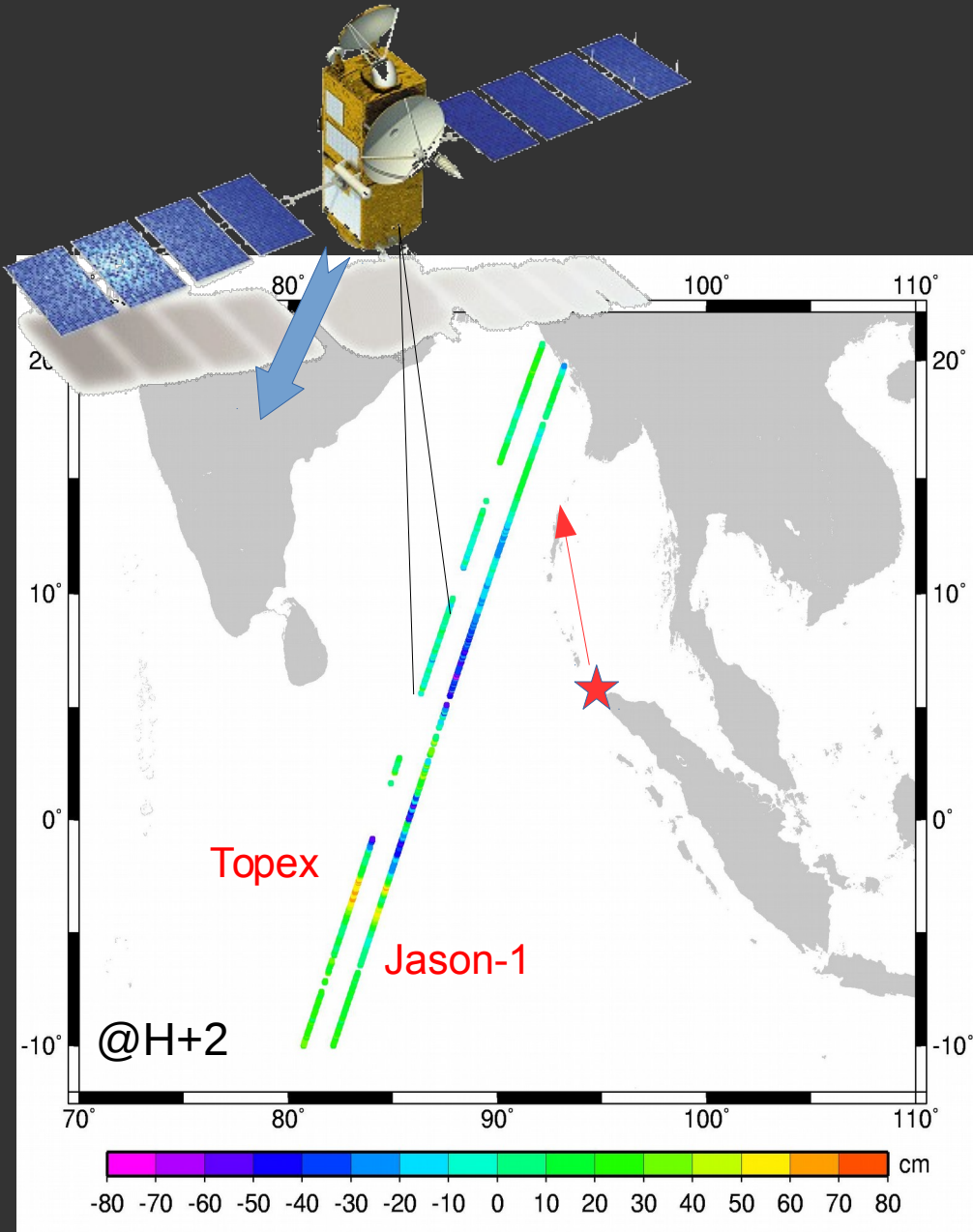
Tide gage data today



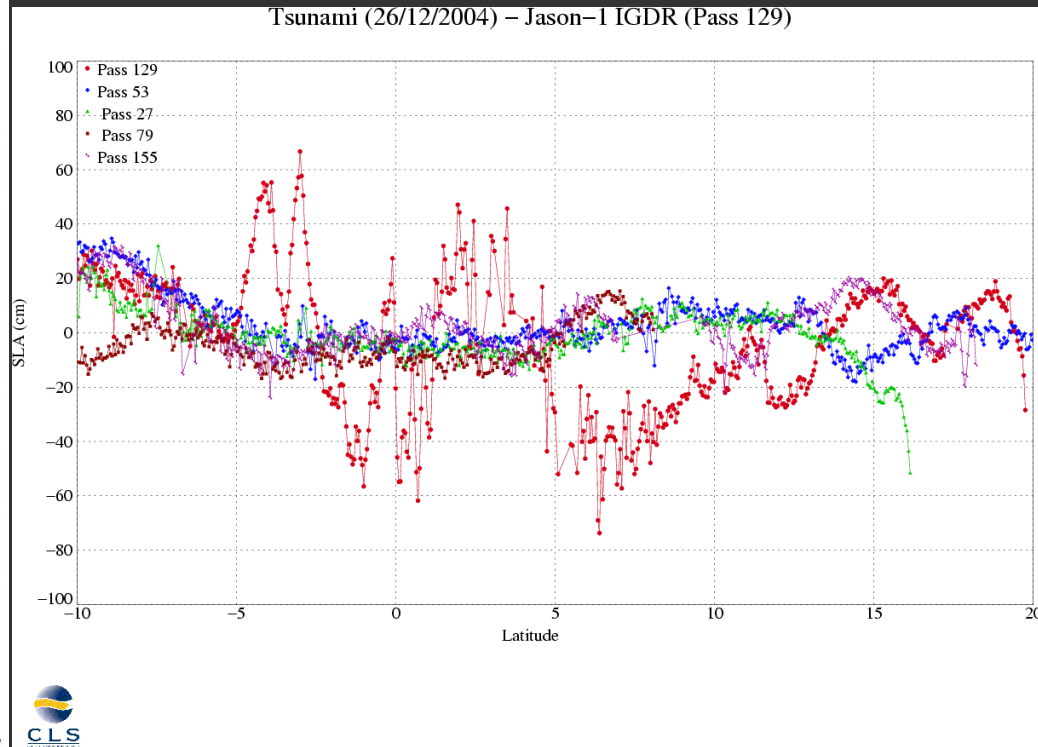
- ✓ Good global coverage,
- ✓ increasing number of stations with rapid sampling ($>1/10\text{min}$),
- ✗ cannot record big waves,
- ✗ deep inside harbors, bays to record only tides



Altimetry data of M9.2 Sumatra 2004

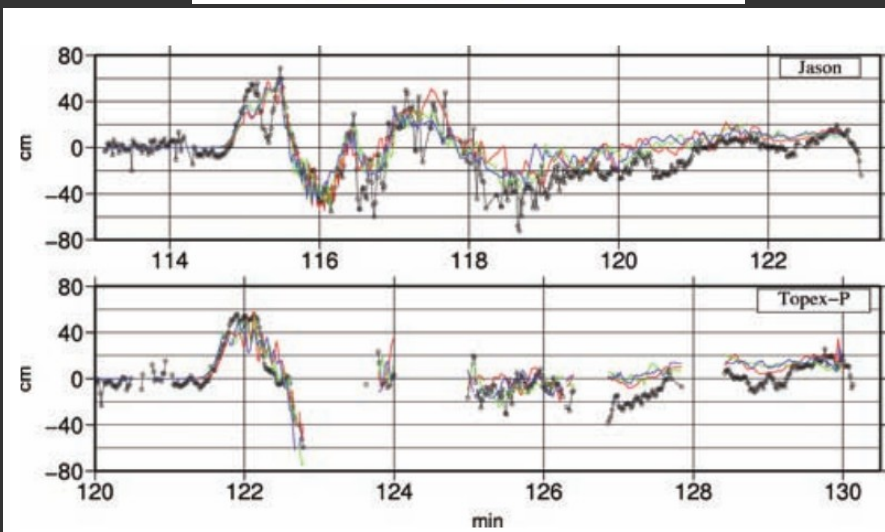
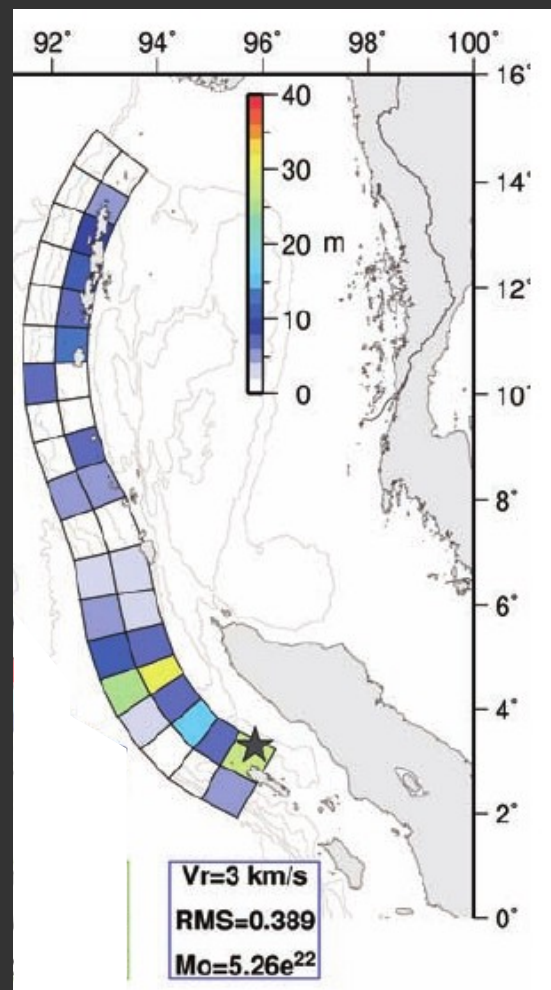
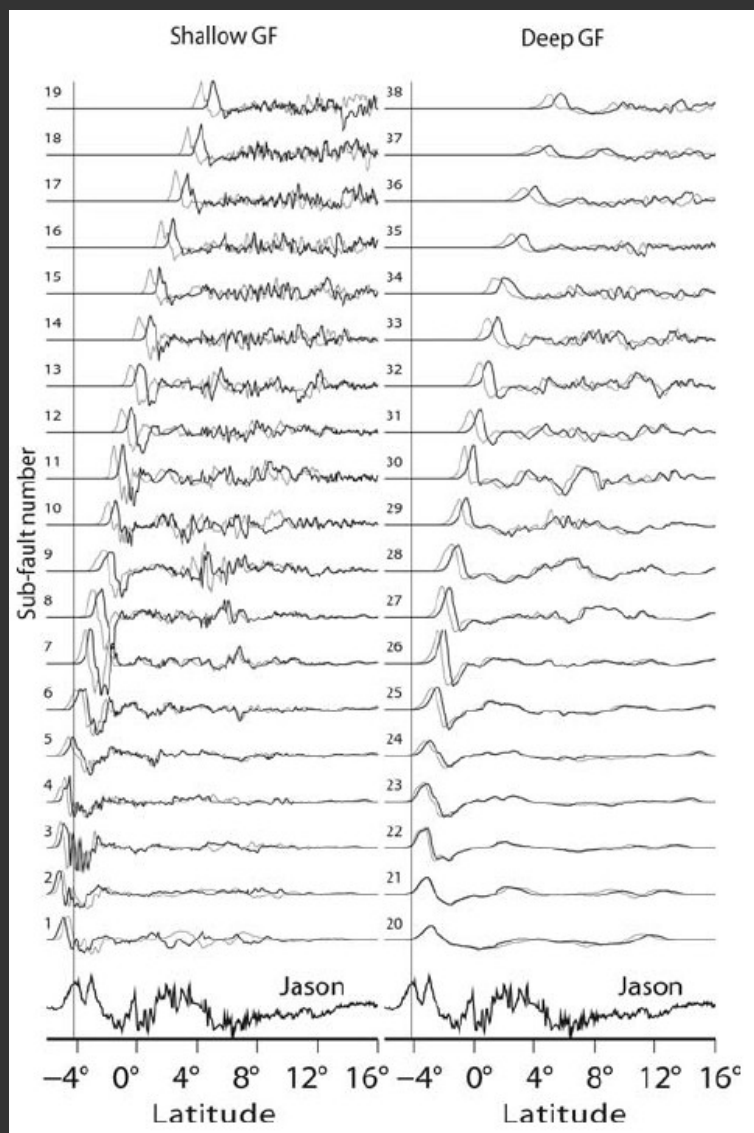


No coastal, harbor
propagation effects !



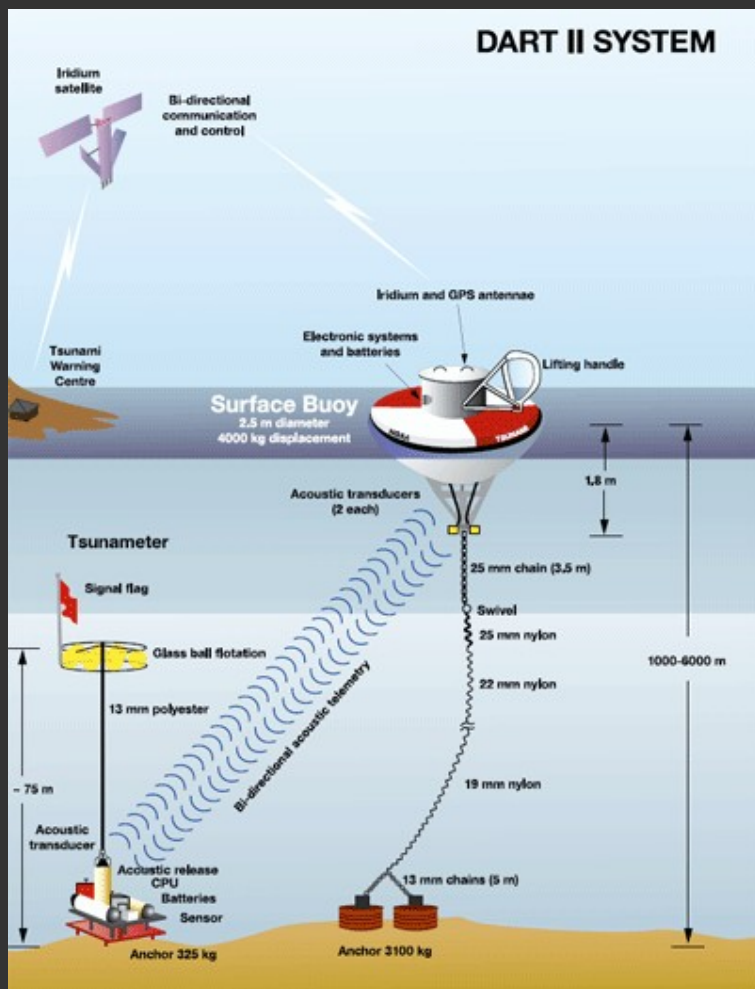
...but quite noisy data

Inversion illustrated

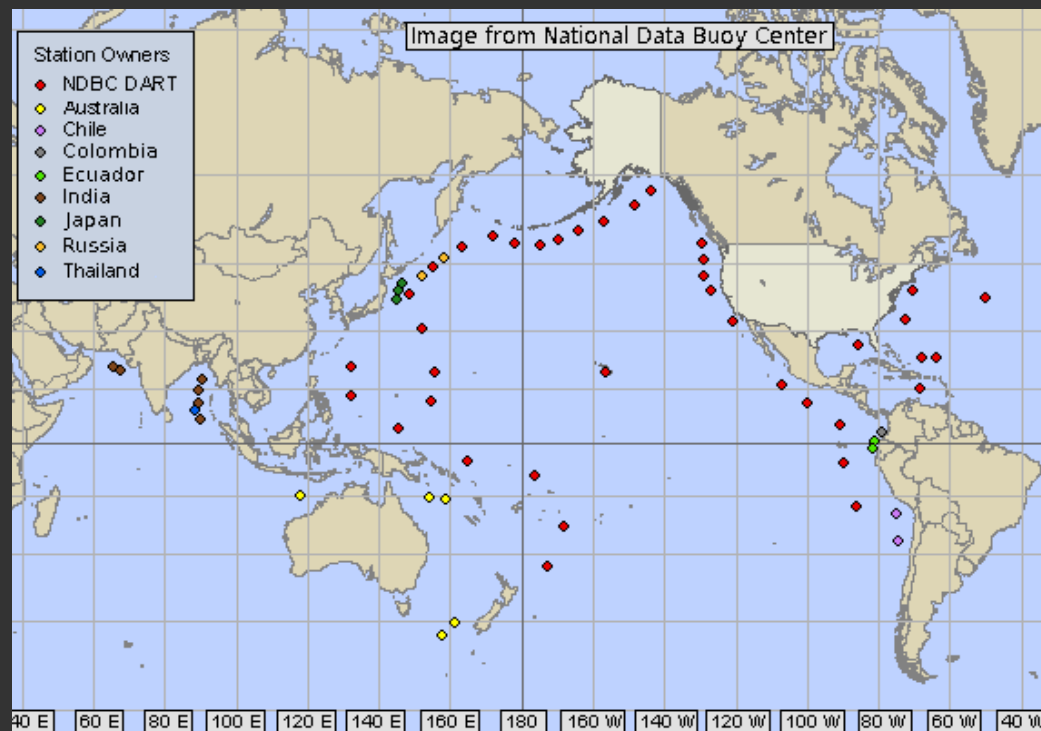


Tsunami data

- Sumatra 2004 triggered the fast development of deep-ocean pressure sensors « DART© buoys »



No effect of surface wave currents

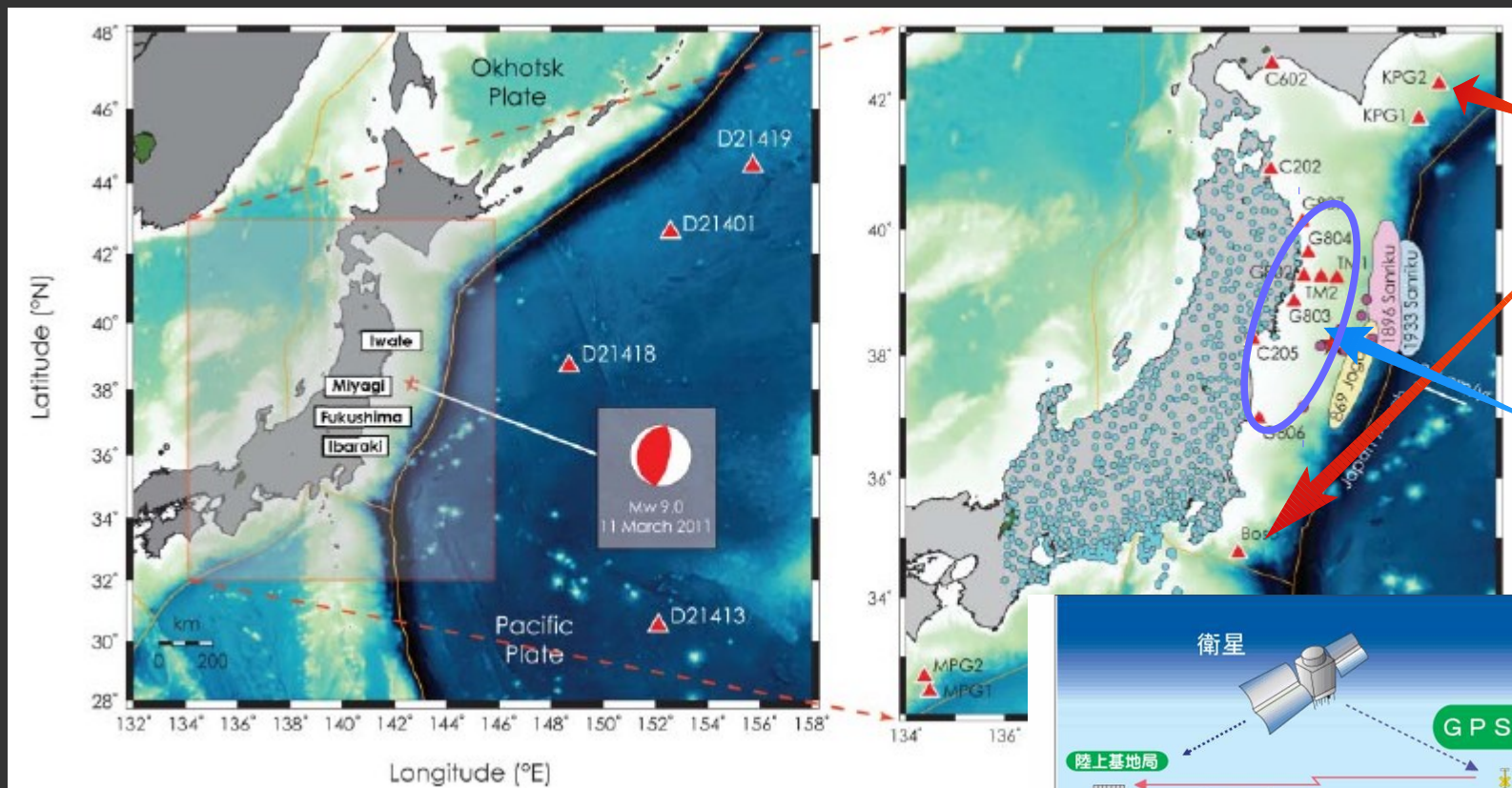


Today's situation (\$\$)

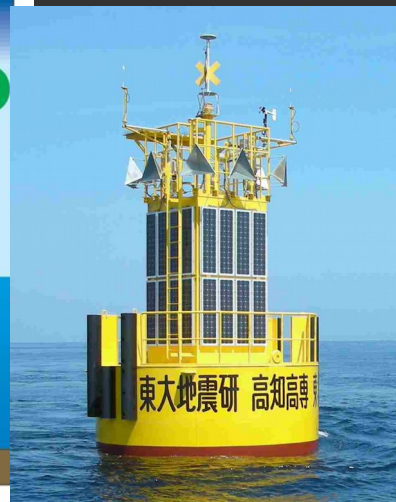
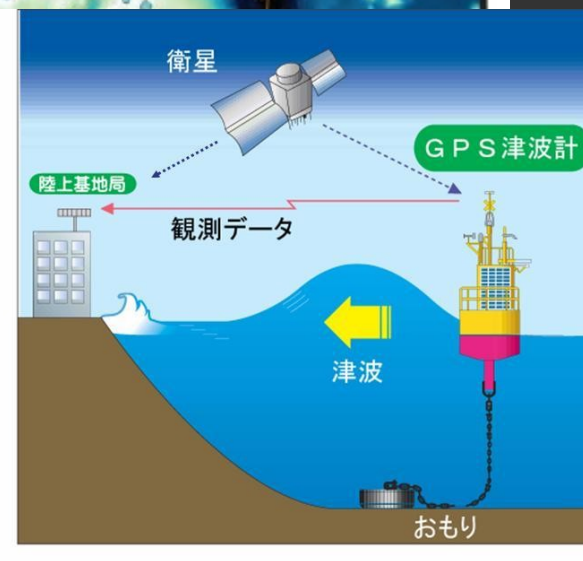
Data directly available online (link)
More and more source studies using these records

2011 M_w 9.0 Japan earthquake

Buoys with pressure sensors



Almost complete azimuthal coverage of the source!

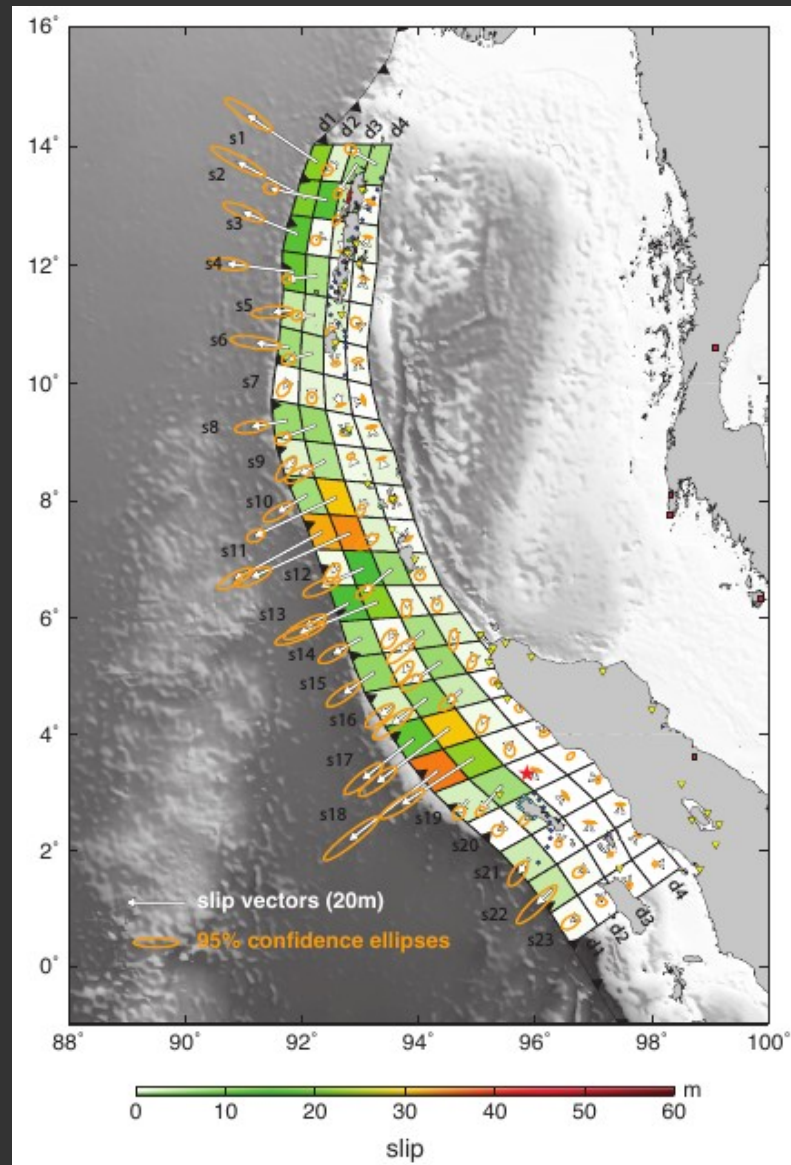
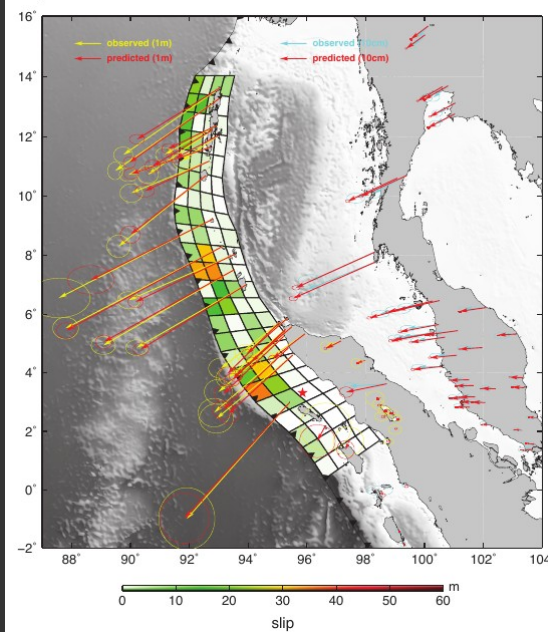
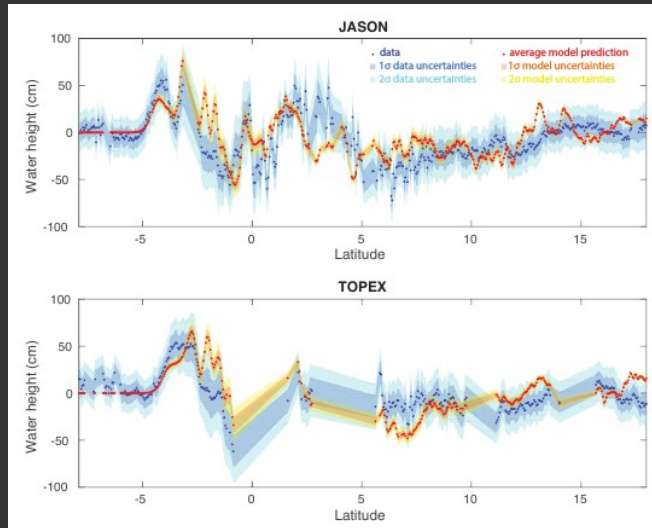


Inversion of tsunami data

- Advantages :
 - linear problem (for the most part),
 - absolute time!!
 - directly probing of sea-bottom deformation, even if rupture is far offshore!!
 - slow enough to assume static source (in most cases): $V_{\text{tsu}} \sim 200\text{m/s}$ and $V_r \sim 3\text{km/s}$

POSTER on Sumatra 2004

bayesian inversion of tsunami and geodetic data

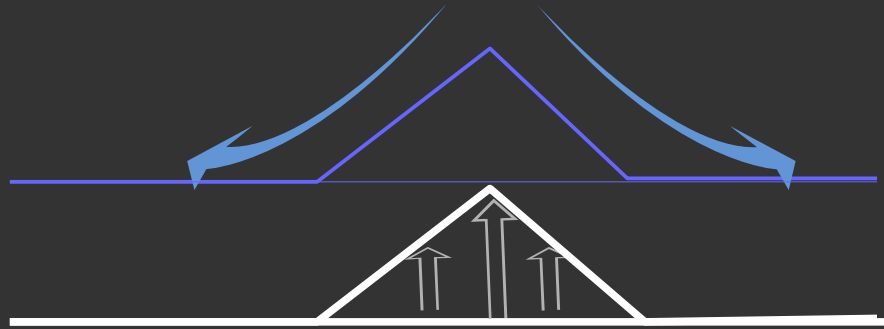


Corrections and limitation

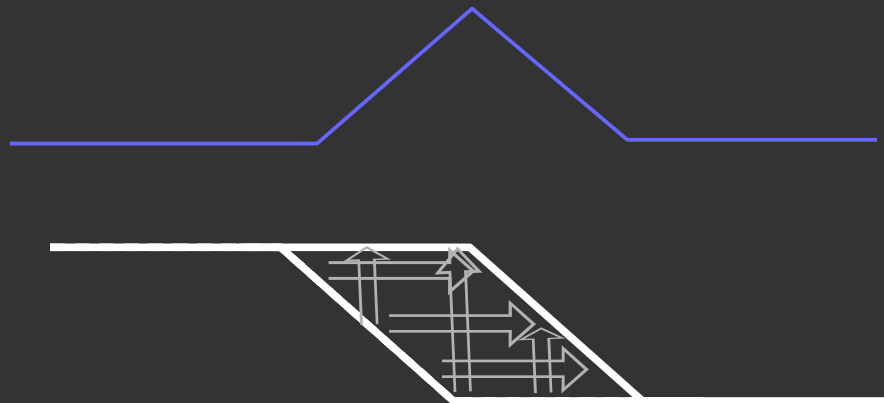
Things you have to check if you get into the buisness

- Water filters $\text{freq} > \text{depth}^3$ (Kajiura, 1963)
- If steep bathymetry: extra vertical displacement from horizontal motion,
- Low and high frequency dispersion,

Bathymetry effect



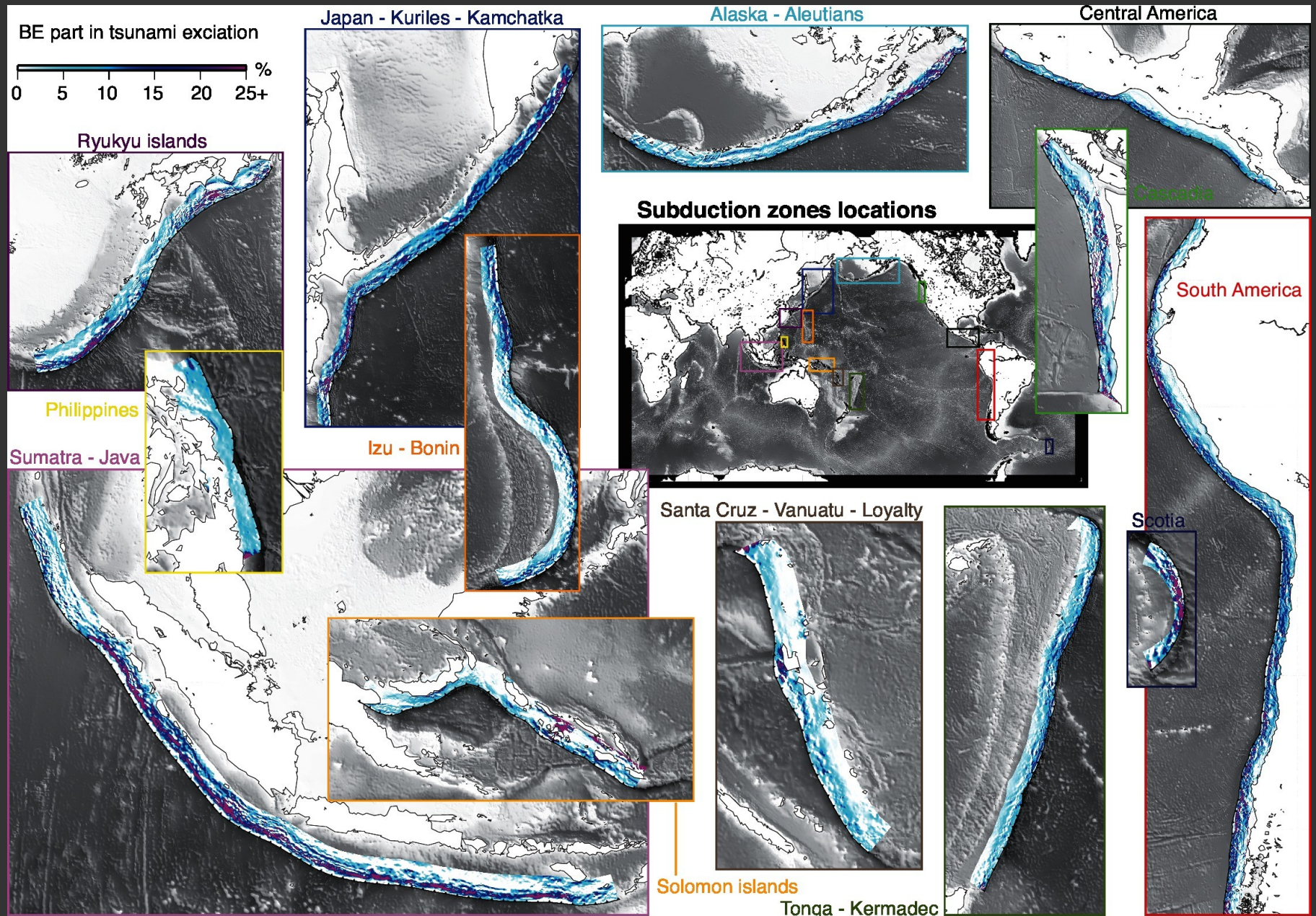
Vertical deformation



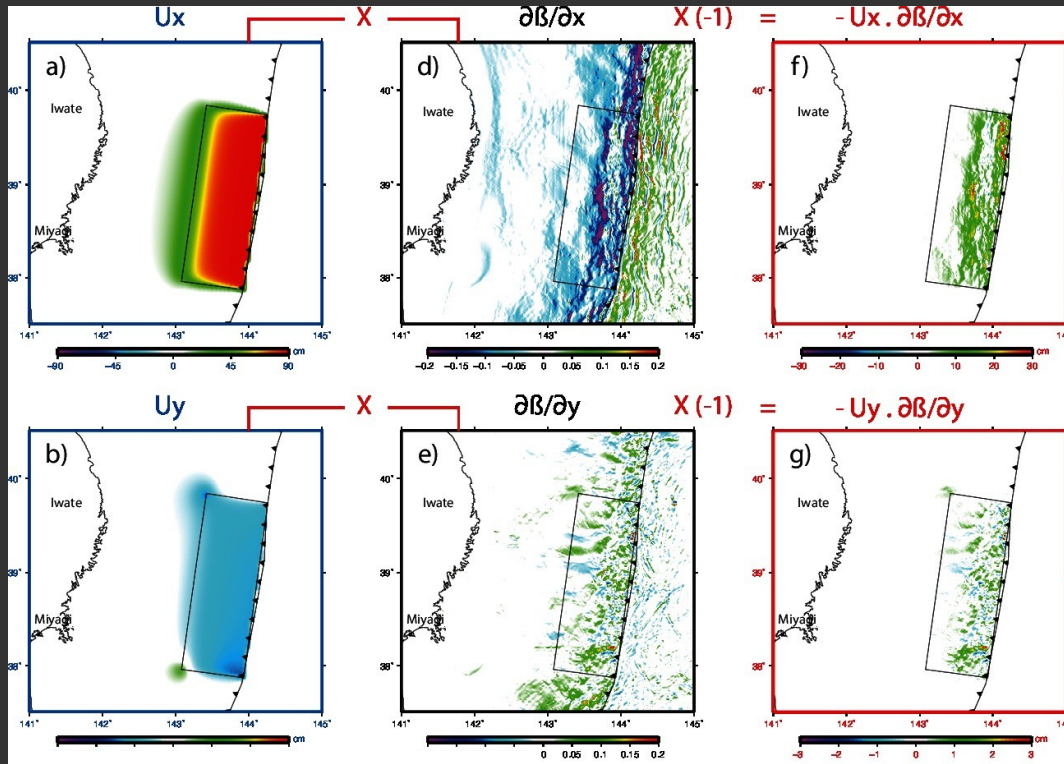
Vertical deformation
from horizontal motion

Tanioka and Satake [1996]

Bathymetric effect at global scale



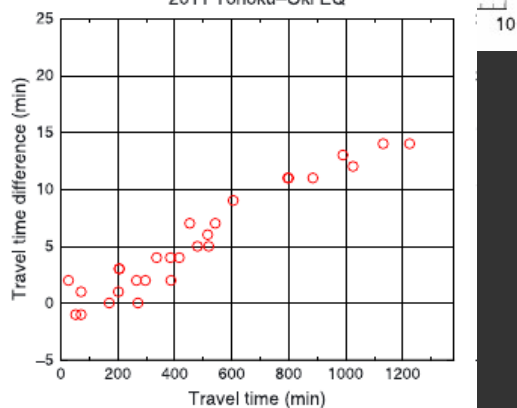
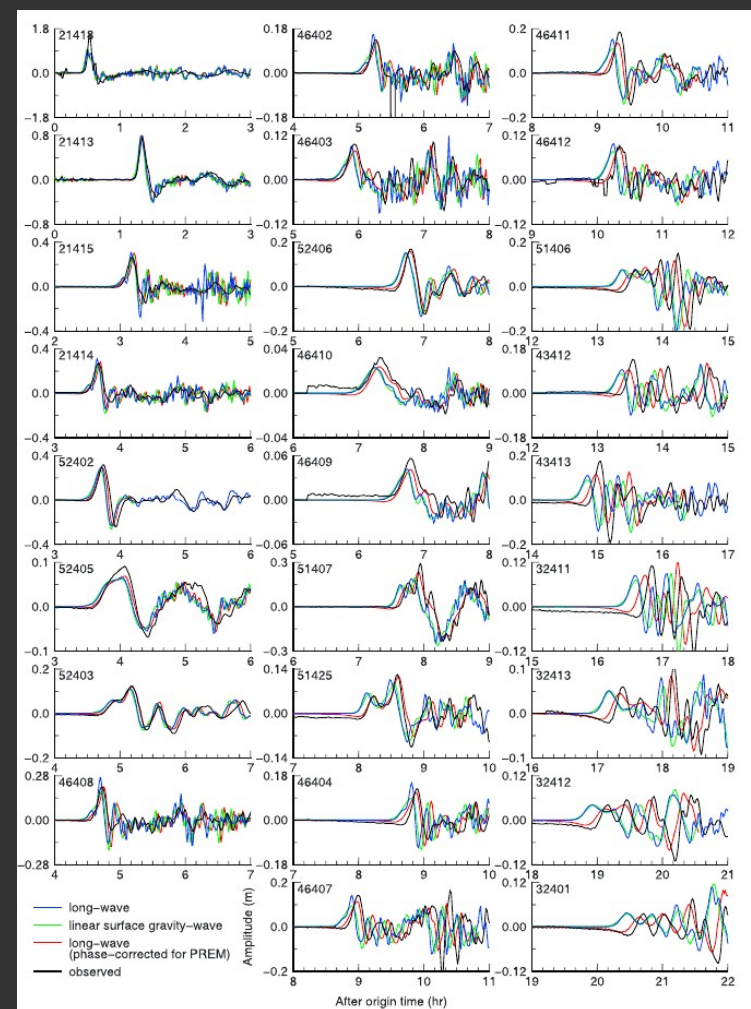
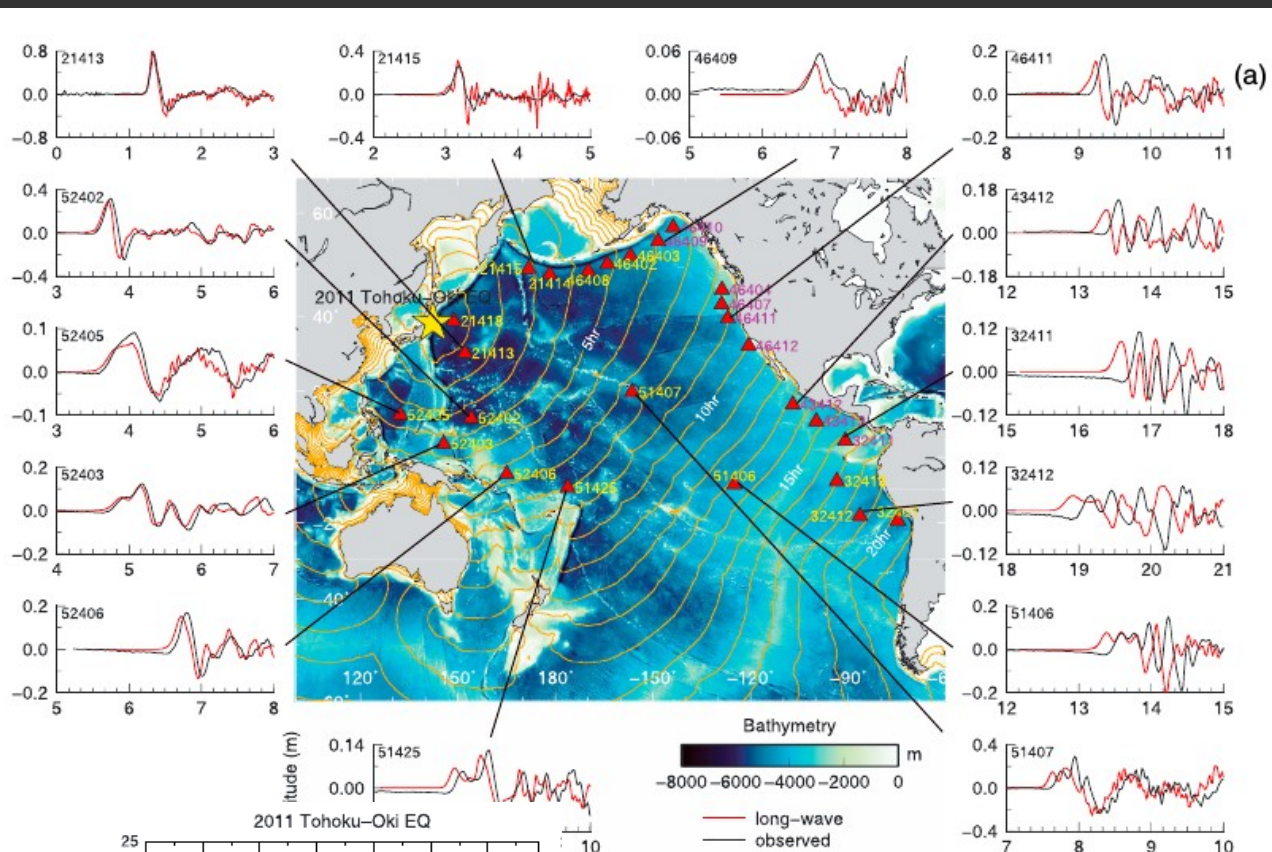
Improving Earth-tsunami coupling



Low frequency dispersion

Dispersion caused by elastic loading
Tsunami speed reduction due to vertical
seawater stratification

After correction from 1D
Earth dispersion curves



Summary on tsunami data

- Tsunami data are critical to characterize old/future subduction earthquakes,
- “Simple” as geodetic data for earthquakes occurring offshore

And now:

- Dvlpt to improve physics in the models, with faster more efficient simulations,
- deep-ocean buoy program is expensive: different group exploring alternatives...

SIMULATION CODES

- **Tunami** (Univ. Tohoku): FD shallow-water eq., multi-grid, bottom roughness,
- **COMCOT** (Univ. Cornell): FD shallow-water eq., multi-grid, bottom roughness,
- **Geoclaw** (Univ. Washington): subpackage of Clawpack for tsunami. FV shallow-water, adaptative mesh,
- **NEOWAVE** (Univ. Hawaii) : FD non-hydrostatic SW equations, 2-way nested grid. Distributed upon request.

Summary

SAFETY NET

To detect tsunamis, Japan plans to deploy 154 observing posts linked by sea-floor cables by 2016. This year, it will install three buoys that will relay information from deep-sea tsunami sensors.

